# Compensating \& Equivalent Variations, Substitution \& Income Effects 

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Figure 1: Suppose a consumer has preferences of the form $U(x, y)=x^{0.5} y^{0.5}$. The price of good $y$ is 1 and the price of good $x$ changes from 1 to 2 . The consumer has income $m=8$. Assuming the consumer is utility maximizing, calculate the Compensating Variation and Equivalent Variation of the price change. Finally, decompose the total change in demand for good $x$ into a substitution effect and an income effect.


Figure 1:
$e_{0}$ : initial equilibrium
$e_{1}$ : final equilibrium (after price of $x$ increases)

$$
\begin{aligned}
& e_{2}: \mathrm{CV} \text { adjustment } \\
& e_{e}: \mathrm{EV} \text { adjustment }
\end{aligned}
$$

Figure 2: Consider the utility function $U(x, y)=x^{0.5}+y$. Suppose that income $m=4$, the price of good $y$ is 1 and the price of good $x$ is 0.25 . If the price of $\operatorname{good} x$ changes from 0.25 to 0.5 , calculate the Compensating Variation and Equivalent Variation of the price change, and decompose the total change in demand for good $x$ into a substitution effect and an income effect.


Total Effect

Figure 2:
$e_{0}$ : initial equilibrium
$e_{1}$ : final equilibrium (after price of $x$ increases)
$e_{2}$ : CV adjustment
$e_{e}$ : EV adjustment

